Day #43 Homework

A particle moves along the x axis such that its position, for t > 0, is given by the function $p(t) = e^{2t} - 5t$. Use this information to complete exercises 1-4.

What are the values of p'(2) and p''(2)? Explain what each value represents.

p'(+) = 2e2+-5 p"(+) = 4e2+

p1(2)= 2e -5 p11(2)= 4e4

P(2) represents the velocity and P(2) represents the acceleration of the particle at t=2.

2. Based on the values found in part (a), what can be concluded about the speed of the particle at t = 2? Give a reason for your answer.

Since p(2) >0 and p((2) >0, the speed of the particle is increasing at t=2.

On what interval(s) of t is the particle moving to the left? To the right? Justify your answers.

p(t) = 0 2=26-5=0 0 Neg 0.458 Pos

p2t = 5/2 2t= Jn(5/2)

Since p'(t) <0, the particle is moving left on oct <0.458. Since p(t)>0, the

t = 0.458 particle is moving right on t > 0.458.

4. Does the particle ever change directions? Justify your answer.

Since p(t) = v(t) changes signs at t=0.458, the particle changes directions.

 The graph of v(t), the velocity of a moving particle, is given below. What conclusions can be made about the movement of the particle along the x – axis and the acceleration, a(t), of the particle for t > 0? Give reasons for your answers.

Since v(t) <0 on Oct<2, the particle is moving to the left.

Since v(t) > 0 for t>2, the particle is moving to the right. Since v(t) is always increasing, etten a(t) is always positive for t >0.

6. If the position of a particle is defined by the function $x(t) = t^3 - 9t^2 + 24t$ for t > 0, is the speed of the particle increasing or decreasing when t = 2.5? Justify your answer.

$$\chi'(t) = \chi(t) = 3t^2 - 18t + 24$$
 $\chi''(t) = \alpha(t) = 6t - 18$
 $\chi'(2.5) = 3(2.5)^2 - 18(2.5) + 24$ $\alpha(2.5) = 6(2.5) - 18$
 $\chi(2.5) = -2.25$ $\alpha(2.5) = -3$

Since both v(2.5) and a(2.5) < 0, the speed of the particle is increasing at t=2.5.

The position of a particle is given by the function $p(t) = (2t - 3)e^{2-t}$ for t > 0. Answer questions 7 - 9.

7. What is the average velocity from t = 1 to t = 3?

Average velocity =
$$\frac{p(1)-p(3)}{1-3}=1.911$$

8. Find an equation for v(t), the velocity of the particle.

$$p'(t) = v(t) = 2e^{2-t} + -1(2t-3)e^{2-t}$$

$$v(t) = 2e^{2-t} - (2t-3)e^{2-t}$$

$$v(t) = e^{2-t} (2-2t+3)$$

$$v(t) = (5-2t)e^{2-t}$$

9. For what value(s) of t will the v(t) = 0?

$$V(t)=0$$

 $5-2t=0$ $e^{2-t}=0$
 $-2t=-5$ $2-t=\ln 0$
 $t=\frac{1}{2}$ $t=\frac{1}{2}$