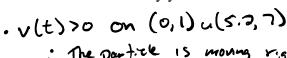
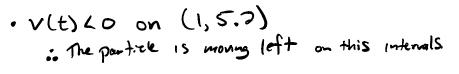
Homework 5.5

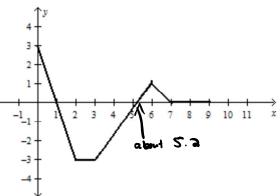
The function whose graph is pictured below, represents the velocity, v(t), of a particle for t = 0 to t = 9 seconds moving along the x – axis. Use the graph to complete exercises 1 - 4.

1. On what interval(s) is the particle moving to the right? Left? Justify your answer.



.. The pointick is moving right on these internals





2. On what interval(s) is the particle slowing down? Speeding up? Justify your answer.

v(t) >0 when v(t) is above t-axis. v(t) <0 when v(t) is below t-axis.

a(t) >0 when v(t) is increasing.

a(t) <0 when v(t) is decreasing.

· The particle is sluwing dawn when v(t) and a(t) are opposite signs.

v(t) > 0 and a(t) < 0 on (0,1) u(6,7)v(t) < 0 and a(t) > 0 on (3,5.2)

: The particle 15 Slaving dans on (0,1), (3,5,7) 4 (4,7)

• The particle is speeding up when v(t) and alt) are the same signs.

v(t) > 0 and a(t) > 0 on (5.2,4)v(t) < 0 and a(t) < 0 on (1.2)

in the particle is speeding up on (1,2) and (5.2,4)

3. At what value(s) of *t* is the particle momentarily stopped and changing directions? Justify your answer.

v(t) crosses the t-axis at t=1 and t=5.2

.. The particle momentarily stops and changes direction at t=1 ant=5.2

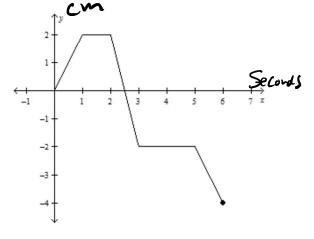
4. On what interval of the time is the acceleration 0? Justify your answer.

v(t) is constant on (2,3) and (7,9)

· alt = 0 on these intervals.

The graph below represents the position, p(t), of a particle that is moving along the x – axis on the interval $0 \le t \le 6$. Use the graph to complete exercises 5 - 9. p(t) is measured in centimeters and t is measured in seconds.

5. For what interval(s) of time is the particle moving to the right? Justify your answer.



6. For what interval(s) of time is the particle moving to the left? Justify your answer.

7. Express the velocity, v(t), as a piecewise-defined function on the interval $0 \le t \le 6$.

$$v(t) = \begin{cases} 2, & 0 < t < 1 \\ 0, & 1 < t < 2 \end{cases}$$
 $0, & 3 < t < 6 \end{cases}$
 $0, & 3 < 6 < 6 < 6 \end{cases}$

8. At what value(s) of t is the velocity undefined on the interval 1 < t < 6? Graphically justify your reasoning.

p(t) hes (asps at
$$t=2$$
, $t=3$, and $t=5$
: $v(t)$ is undefined at $t=2$, $t=3$, and $t=5$

9. Find the average velocity of the particle on the interval $1 \le t \le 6$.

Average Velocity on [1,4] =
$$\frac{p(1)-p(4)}{1-6} = \frac{2-(-4)}{-5} = \frac{6}{-5} \text{ cm/gc}$$

A particle moves along the x – axis so that at any time $0 \le t \le 5$, the velocity, in meters per second, is given by the function $v(t) = (t-2)^2 \cos(2t)$. Use a graphing calculator to complete exercises 10-12. $2(t-3)^2(t) \le (t-3)^3(-\sin(2t) \cdot 2)$

10. On the interval $0 \le t \le 5$, at how many times does the particle change directions? Give a reason for your answer.

V(t) crosses the t-axis at
$$X=\frac{\pi}{4}$$
, $X=3$, $X=\frac{3\pi}{4}$, and $X=\frac{5\pi}{4}$.

The particle changes direction 4 times on $[0,5]$

11. Using appropriate units, what is the value of v'(2). Describe the motion of the particle at this time. Justify your answer.

$$V'(7) = 0$$
 meters/second²
 $V'(7) = 0$ and $V(7) = 0$
.: The particle is not moving at all.

12. Using appropriate units, what is the average acceleration between t = 1 and t = 3.5 seconds?

Average Acceleration on (1,3.5) =
$$\frac{V(1) - V(3.5)}{1 - 3.5} = \frac{-416 - 1.696}{-2.5} = \frac{-2.112}{-2.5}$$

$$\approx 0.845 \text{ metrs/Secont}^2$$

13. What is the acceleration of the particle the first time that the velocity is 0?

The first time V(t) = 0 is when $t = \frac{\pi}{4}$

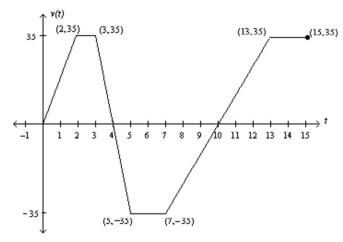
$$a(t) = 2(t-3)'(1) \cos(2t) + (t-3)^{2} (-\sin(2t) \cdot 2)$$

$$a(t) = 2(t-3) \cos(2t) - 2(t-3)^{2} \sin(2t)$$

$$a(\frac{\pi}{4}) = 2(\frac{\pi}{4} - 3) \cos(2\frac{\pi}{4}) - 2(\frac{\pi}{4} - 3)^{2} \sin(2\frac{\pi}{4})$$

$$a(\frac{\pi}{4}) \approx -2.951$$

Jeff leaves his house riding his bicycle toward school. His velocity v(t), measured in feet per minute, on the interval 0 < t < 15, for t minutes, is shown in the graph to the right. Use the graph to complete exercises 14 - 17.



14. Find the value of
$$v'(4)$$
. Explain, using appropriate units, what this value represents.
$$v'(4) = \frac{35 - (-35)}{3 - 5} = \frac{70}{-2} = -35 \text{ feet/min}^2$$

Four minutes after leaving home, Jeff's acceleration is -35 feet/min?

15. On the interval $0 \le t \le 5$, is there any interval of time at which a(t) = 0? Explain how you know.

v(t) is constant on
$$(2.3)$$

: $a(t) = 0$ on (2.3)

16. On the interval $0 \le t \le 5$, does Rolle's Theorem guarantee that there will be a value of t such that a(t) = 0? Justify your answer.

17. At some point, Jeff realizes that he forgot something at home and has to turn around. After how many minutes does he turn around? Give a reason for your answer.