Part II: Integrate each definite integral with u-substitution. #1) $\int_0^2 (x^2 - 1)^5 2x \, dx$

$$u = x - 1$$

$$\frac{dy}{dx} = 2x$$

$$du = 2x dx$$

$$\frac{dy}{dx} = dx$$

$$= \frac{3}{3} u^{5} = \frac{3}{3} u^$$

#2)
$$\int_{0}^{1} e^{x^{2}} 2x \, dx = \int_{e}^{u} \int_{x} \left(\frac{du}{2x}\right)$$

$$= \int_{e}^{u} du$$

#3)
$$\int_{-3}^{3} \frac{2x}{x^{2}-1} dx = \int_{-3}^{3} \frac{du}{u}$$

$$= \int_{-3}^{3} \frac{du}{x^{2}-1} dx$$

$$= \int_{-3}^{3} \frac{du}{u} du$$

#4)
$$\int_{-1}^{1} (x^{2} - 1)^{5}x \, dx = \int_{0}^{\infty} u^{5} \left(\frac{du}{2} \right)^{5}$$

$$u = x^{2} - 1$$

$$\frac{du}{dx} = 0$$

$$du = 0$$

#5)
$$\int_{1}^{2} e^{x^{3}} 3x^{2} dx = \int_{e^{1}}^{2} \frac{dy}{3x^{3}}$$

$$\frac{dy}{dx} = 3x^{3} dx$$

$$\frac{dy}{3x^{2}} = dx$$

$$= e^{3} - e$$

$$= e^{3} - e$$

#6)
$$\int_{-2}^{2} \frac{x^{2}}{x^{3}+2} dx = \int_{-1}^{2} \frac{du}{(\frac{du}{3}x^{5})}$$

$$= \frac{1}{3} \int_{-1}^{2} \frac{du}{du}$$

Bathroom Tissue

#7) Adding to his line of products for *The Slightly Used Company*, George starts selling bathroom tissue. *Slightly Used's* marginal cost function is $MC(x) = \frac{1}{4x+2}$ and its fixed costs are \$4. Find the cost function.

$$C(x) = \sum_{y \in A} C(x) dx$$

$$= \int_{4x+2}^{1} dx$$

$$= \int_{4x+2}^{1} dx$$

$$= \int_{4}^{1} \left(\frac{dy}{4} \right)$$

$$= \int_{4}^{1} \int_{4x+2}^{1} dx$$

$$= \int_{4}^{1} \ln |u| + C$$

$$C(x) = \int_{4}^{1} \ln |4x+2| + C$$

$$H = \int_{4}^{1} \ln |2| + C$$

$$H = \int_{6}^{1} \ln |2| + C$$

$$I(6-1n) = C$$

$$C(x) = \int_{4}^{1} \ln |4x+2| + I(6-1n)$$

Pluckable Hairs

#8) The number of pluckable hairs on George's ears is expected to be $P(x) = x(x^2 + 4)^{-1/2}$ hairs after x months. Find the average number of pluckable hairs between month x = 0 and month x = 8.

month
$$x = 0$$
 and month $x = 8$.

A verage Pluckable Hars = $\frac{1}{8} \cdot \frac{1}{2} \cdot \frac{1}$

Average Pluckoble Hars = 78 per month

The average number of pluckable hairs from month

Alliteration - The Prequel

#9) George sells sails for snail sized sailboats. His sales of sails for snail sized sailboats during week x are given by $S(x) = \frac{1}{x+4}$ in hundreds. Find the average sales of sails for snail sized sailboats from week x = 1 to week x = 4. (Don't forget your answer is in hundreds, noob.)

The overage sales of sails was 12 from week 1 44.

Alliteration

#10) An experimental therapy lowers a patient's patience for patterns at the rate of $t\sqrt{36-t^2}$ units per day, where t is the number of days since the therapy was administered (for the first six days). Find the total change in a patient's patience for patterns during the first 3 days.

A patient's patience for patturns lowers by about 25 units during the first 3 days.

Condiments

#11) George has developed a new business model for making money in the restaurant business – give away the food for free, but charge for the condiments. He is selling condiments at the rate of $100e^{-x}$ per week after x weeks. How many condiments will be sold during the first 8 weeks?

$$C = \frac{8}{100} \cdot \frac{1}{100} \cdot$$

George will sell 100 condiments during the first week.

Discharging Pits

#12) George's armpits are discharging pollution into the air at the rate of r(t) liters per year given by $r(t) = \frac{1}{t+1}$ where t is the number of years since George washed. Find the total amount of pollution discharged during the first 3 years of not washing.

George's armpits have sent 1.4 liters of pollution into the air during the first 3 years.