Follow the directions to answer each of the following problems. Only use your calculator when a problem displays the calculator icon.

Topic 4.1 & 4.3 Interpreting the Meaning of a Derivative in Context; **Rates of Change in Applied Contexts Other Than Motion** rat in

Eager rock fans enter a line to buy tickets to see the renowned band, Sir Isaac & the Newtones at a rate 1. modeled by the function given by $E(t) = 512.7e^{-0.173t}$ where E(t) is measured in people per minute and t is measured in minutes for the interval $0 \le t \le 30$. Find E'(22) and using correct units, interpret its meaning in the context of the problem. N The rate at which people are entering $\frac{d}{dX}(512.7\mathrm{e}^{-.173X})_{X=22}$ U is decreasing by 1.972 people/min2

Topic 4.2 Straight Line Motion: Connecting Position, Velocity and Acceleration

T at 22 minutes

2. The graph below shows the velocity, v(t), of a particle moving along the x-axis and can be defined by a continuous linear piecewise-defined function over the interval $0 \le t \le 9$. Note that v'(t) = 0 on 3 < x < 4.

-1.972352907

a. Over which time interval(s) does the particle move to the left? Justify your answer.

b. Over which time interval(s) is the particle speeding up? Justify your answer.

c. Over which time interval(s) is the particle's speed decreasing? Justify your answer.

Hw

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dr = 3 ft/sec

Topics 4.4 & 4.5: Related Rates 3. If $\sqrt{x} + y = 6$ and $\frac{dy}{dt} = 2$, find $\frac{dx}{dt}$ when x = 4. $\frac{dy}{dt} = \sqrt{1 + 1} = 0$ $\frac{1}{2}\sqrt{1 + 1} = \frac{1}{4t} = 0$ $\frac{1}{2}\sqrt{1 + 1} = \frac{1}{4t} = -2$ $\frac{dy}{dt} = -2$

4. A kite is flying at a height of 40 ft. A child is flying it so that it is moving horizontally at a rate of 3 ft/sec. If the string is taut, at what rate is the string being let out when the length of the string released is 50 ft?

$$d_{\text{ott}} \left(\chi^{2} + 4\upsilon^{2} = 2^{2} \right)$$

$$d_{\text{ott}} \left(\chi^{2} + 4\upsilon^{2} = 2^{2} \frac{d^{2}}{dt} \right)$$

$$2\chi_{\text{ott}}^{\text{ott}} = 22 \frac{d^{2}}{dt}$$

$$2\chi(3) = 22 \frac{d^{2}}{dt}$$

$$\frac{1}{30} \qquad Find \frac{d^2}{dt} |_{z=50}$$

$$\frac{50}{30} 40$$

$$\frac{2 \cdot 30 \cdot 3}{3 \cdot 30} = \frac{d^2}{dt}$$

$$\frac{3 \cdot 30 \cdot 3}{5 \cdot 50} = \frac{d^2}{dt}$$

$$\frac{9}{5} \frac{Ft/st}{5} = \frac{d^2}{dt}$$

Hw

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The volume of a sphere is $V = \frac{4}{3}\pi r^3$.



1

$$\frac{d}{dt}\left(V = \frac{4}{3}\pi r^{3}\right)$$
$$\frac{dV}{dt} = 4\pi r^{2}\frac{dr}{dt}$$
$$8 = 4\pi r^{2}\frac{dr}{dt}$$

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$$\begin{array}{c|c} \hline & F(ND) \frac{dr}{dt} \\ \gamma = 2 \end{array} & \begin{array}{c} 8 = 4 fr (2)^2 \frac{dr}{dt} \\ \frac{87}{4fr \cdot 4} = \frac{dr}{dt} \\ \frac{dr}{dt} = \frac{1}{2fr} \frac{fr}{ft} / min \end{array}$$

6. Sand is being dropped onto a conical pile at a rate of 10 cubic meters per minute. If the height of the pile always twice the base radius, at what rate is the height increasing when the pile is 8 m high?

The volume of a cone is
$$V = \frac{1}{3}\pi r^2 h$$
.

$$V = \frac{1}{3}\pi \left(\frac{h}{2}\right)^2 h$$

$$\begin{bmatrix} 1 \land D & \frac{dh}{dt} \\ h = 8 \end{bmatrix} \qquad \begin{bmatrix} 10 & = \frac{1}{4} \land (8)^2 \frac{dh}{dt} \\ 10 & = \frac{1}{5} \land \pi \cdot 8^2 \cdot 8 \frac{dh}{dt} \\ \frac{10}{16 \land \pi} & = \frac{dh}{dt} \\ \frac{5}{8 \land \pi} m/_{min} & = \frac{dh}{dt} \end{bmatrix}$$

7. The volume of a cube is increasing by 10 cm³/min. Find the rate the surface area is increasing when the side of the cube is 5 cm.



$$\frac{d}{dt}\left(v = x^{3}\right) \qquad \frac{d}{dt}\left(A = 6x^{2}\right)$$

$$\frac{d}{dt}\left(A = 6x^{2}\right)$$

$$\frac{d}{dt} = 3x^{2} \cdot \frac{dx}{dt} \qquad \frac{dA}{dt} = 13x \cdot \frac{dx}{dt}$$

$$\frac{10}{3x^{2}} = \frac{dx}{dt} \qquad \frac{dA}{dt} = 13x \cdot \frac{10}{3x^{2}}$$

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$$\begin{array}{c} \hline \\ Find \frac{dA}{dt} \\ x=5 \end{array}$$

$$\frac{dA}{dt} = \frac{40}{x}$$

$$\frac{dA}{dt} = \frac{40}{x}$$

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.

a.) At the instant when the radius of the oil slick is 100 centimeters and the height is 0.5 centimeter, the radius is increasing at the rate of 2.5 centimeters per minute. At this instant, what is the rate of change of the height of the oil slick with respect to time, in centimeters per minute?

$$\frac{dV}{dt} = 2000 \text{ cm}^{3}/_{min}$$

$$\frac{d}{dt} \left(V = frr^{2}h\right)$$

$$\frac{dV}{dt} = 2frr \cdot \frac{dr}{dt} \cdot h + 2frr^{2} \frac{dh}{dt}$$

$$\frac{dV}{dt} = 2frr \cdot \frac{dr}{dt} \cdot h + 2frr^{2} \frac{dh}{dt}$$

$$\frac{dV}{dt} = 2fr(loo) 2 \cdot 5 \cdot \frac{1}{5} + fr(loo)^{2} \frac{dh}{dt}$$

$$\frac{dr}{dt} = 2 \cdot 5 \text{ cm}/_{min}$$

$$\frac{dr}{dt} = 2 \cdot 5 \text{ cm}/_{min}$$

b.) A recovery device arrives on the scene and begins removing oil. The rate at which oil is removed $R(t) = 400\sqrt{t}$ cubic centimeters per minute, where t is the time in minutes since the device began working. Oil continues to leak at a rate of 2000 cubic centimeters per minute. Find the time t when the oil slick is not changing volume.

OIL Leaking = increasing volume of sprill =
$$\pm 2000 \text{ cm}^3/\text{min}$$

OIL Remaral = decreasing volume of sprill = $400Jt$
IN = $0UT$
2000 = $400Jt$
 $S = Jt$
 $2S = t$
 $t = 25 \text{ minutes}$

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Hw

Topic 4.6: Linear Approximation

9. Use the tangent line approximation for
$$f(x) = \sqrt{x}$$
 at $x = 64$ to approximate $\sqrt{65} - \sqrt{63}$.
(A) 0 (B) $\frac{1}{32}$
(C) $\frac{1}{16}$ (D) $\frac{1}{8}$

Q. Let g be a function given by $g(x) = x \cdot f(x)$. If f(-1) = 3 and f'(-1) = -2, use the tangent line to g at x = -1 to approximate g(-0.9).

$$(A) -2.5 (B) -0.2$$

$$(C) -1.8 (D) 3.5$$

$$\frac{Pot(-1, -3)}{g(-1) = -1 \cdot f(-1)} = \frac{S \circ T}{g'(x) = 1 \cdot f(x) + x \cdot f'(x)} = \frac{f(august)}{y(x) = 1 \cdot f(-1) + (-1) \cdot f'(-1)}$$

$$= -1 \cdot 3 \qquad g'(-1) = 1 \cdot f(-1) + (-1) \cdot f'(-1) \qquad T(x) = -3 + S(x+1)$$

$$g(-1) = -3 = 1 \cdot 3 + (-1)(-2) \qquad T(-0.9) = -3 + S(-0.9+1)$$

$$= -3 + S(-0.9+1)$$

$$= -3 + S(-0.1)$$

$$= -3 + S(-0.1)$$

$$= -3 + S(-0.1)$$

$$= -3 + S(-0.1)$$

$$= -3 + S(-0.5)$$

$$T(-0.9) = -2 \cdot S$$

10 Given a function, f(x), the linear approximation for f(a+0.1) would be given by



Hw

Topic 4.7: Indeterminate Forms & L'Hospital's Rule

13. What is
$$\lim_{x \to 1} \frac{e^{x} - e^{x}}{x^{2} - 1}$$
? = $\lim_{x \to 1} \frac{e^{-e^{x}}}{2x}$
(A) $e^{-e^{x}}$ (B) $1^{-e^{x}} = \frac{e^{-e^{1}}}{2x}$
(C) $\frac{e}{4}$ (D) $0^{-e^{x}} = \frac{e^{-e^{1}}}{2x}$

14. The function *f* is continuous and twice-differentiable for all values *x*, f(0) = 1, f'(0) = 1, and f''(0) = 2. What is The following limit?

$$\lim_{x \to 0} \frac{f(x) - x^{-1}}{\sin(2x) - x^{2} - 2x} ? = \lim_{x \to 0} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) - 2\pi - 2} L^{1} \int_{-\infty}^{\infty} \frac{f(x) - 1}{2 \cdot \cos(2\pi) -$$