Calculus
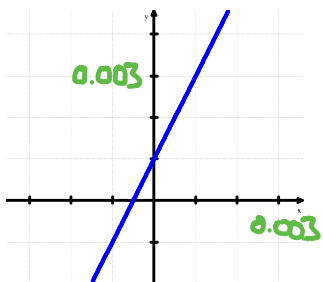
Write your questions
and thoughts here!

2.3 Differentiability

Name:_____

Notes

A graph of a function is shown below. Write down its equation on line #1.

0.003

0.003

1. $y = 2x+1$ (No scale)

2. $y = 2x + 0.001$ (Too much Zoom)

3. $y = \sin(2x) + 0.001$

Differentiability: (Slope)

The derivative exists for each point in the domain. In other words, the graph looks like a line if you zoom in (___local   linearity___).

The derivative ___fails to exist___ where the function has a

1. Discontinuity

2. Corner or cusp point

3. Vertical tangent

True or **False**

Differentiability implies continuity.

True or **False**

Continuity implies differentiability.

NASTY
Theorem

Mean Value Theorem:

If a function f is differentiable (and thereby continuous) over the interval ___(a,b)___, then there exists a point __C__ within that open interval where the instantaneous rate of change equals the average rate of change over the interval.
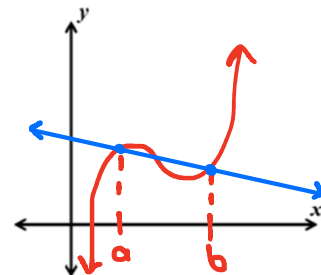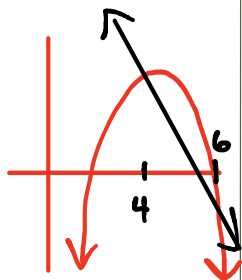
$$f'(c) = ARC(c)$$

2.3 Differentiability

Given $f(x)$ and $f'(x)$ on a given interval $[a, b]$, find a value c that satisfies the Mean Value Theorem.

1. $f(x) = -2x^2 + 16x - 26; \quad 4 \le x \le 6$
   $f'(x) = -4x + 16$

① $f(6) = -2(6)^2 + 16(6) - 26$
   $= -2(36) + 96 - 26$
   $= -72 + 70$
   $f(6) = -2$

② $f(4) = -2(4)^2 + 16(4) - 26$
   $= -2(16) + 64 - 26$
   $= -32 + 38$
   $f(4) = 6$

③ FIND ARC
   $ARC = \dfrac{f(6) - f(4)}{6 - 4}$
   $= \dfrac{(-2) - (6)}{2}$
   $= \dfrac{-8}{2}$
   $ARC = -4$ (slope of secant)

④ Set $ARC = f'(c)$
   $-4 = -4c + 16$
   $-20 = -4c$
   $5 = c$

Derivatives and Calculators:

Using the calculator to find the value of the derivative at a point.

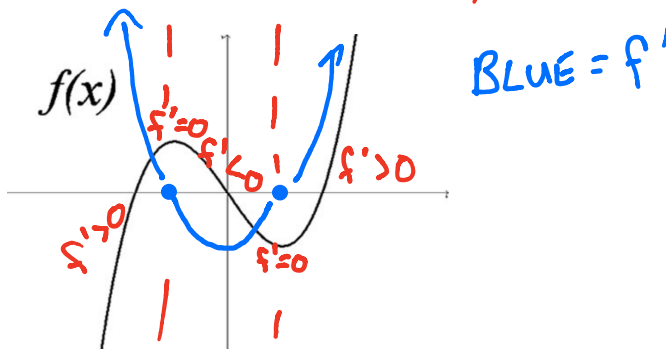2. Find the value of $f'(0.57)$ if $f(x) = \dfrac{x^3}{\ln x}$

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MATH  NUM  CPX nDeriv(X^3/ln(X)
2↑►Dec           ,X,0.57)
3:3                  -2.762240779
4:³√(
5:×√
6:fMin(
7:fMax(
8↓nDeriv(
```

$f'(0.57) = -2.762$

Graph of a function f and its derivative f'

Focus on the __Slope__ of f. The __Slope__ of f is the __y-value__ of f'.

$f(x)$

$f' = 0$ $f' < 0$ $f' > 0$

$f' > 0$ $f' = 0$

BLUE $= f'$