

## 2002 AP Calculus AB #3 (Partial)

An object moves along the  $x$ -axis with initial position  $x(0) = 2$ . The velocity of the object at time  $t \geq 0$  is given by the function  $v(t) = \sin\left(\frac{\pi}{3}t\right)$ .

- a. What is the acceleration of the object at time  $t = 4$ ?

$$v'(t) = a(t) = \cos\left(\frac{\pi}{3}t\right) \cdot \frac{\pi}{3}$$

$$a(4) = \frac{\pi}{3} \cos\left(\frac{\pi}{3} \cdot 4\right)$$

$$= \frac{\pi}{3} \cdot -\frac{1}{2}$$

$$= \boxed{-\frac{\pi}{6}}$$

- b. Consider the following two statements.

Statement I: For  $3 < t < 4.5$ , the velocity of the object is decreasing.

Statement II: For  $3 < t < 4.5$ , the speed of the object is decreasing.

Are either or both of these statements correct? For each statement, provide a reason why it is correct or not correct.

Statement I: since  $v'(4) = a(4) < 0$ , then  $v(t)$  must be decreasing. True

Statement II:  $v(4) = \sin\left(\frac{\pi}{3} \cdot 4\right) = -\frac{\sqrt{3}}{2} < 0$ .  
This statement is false b/c speed is increasing since  $a(4)$  and  $v(4)$  are the same signs.